

Interplay of Touschek scattering, intrabeam scattering, and rf cavities in ultralow-emittance storage rings

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The latest generation of storage ring-based light sources employs multibend achromat lattices to achieve ultralow emittance. These lattices make use of a large number of weak bending magnets which considerably reduces the amount of power radiated in the dipoles in comparison to power radiated from insertion devices. Therefore, in such storage rings, parameters such as emittance, energy spread, and radiated power are—unlike 3rd generation storage rings—no longer constant during a typical user shift. Instead, they depend on several varying parameters such as insertion device gap settings, bunch charge, bunch length, etc. Since the charge per bunch is usually high, intrabeam scattering in medium-energy storage rings with ultralow emittance becomes very strong. This creates a dependence of emittance on stored current. Furthermore, since the bunch length is adjusted with rf cavities but is also varied as insertion device gaps change, the emittance blowup from intrabeam scattering is not constant either. Therefore, the emittance, bunch length, and hence the resulting Touschek lifetime have to be calculated in a self-consistent fashion with 6D tracking taking into account not only the bare lattice and rf cavity settings, but also momentary bunch charge and gap settings. Using the MAX IV 3 GeV storage ring as an example, this paper demonstrates the intricate interplay between transverse emittance (insertion devices, emittance coupling), longitudinal emittance (tuning of main cavities as well as harmonic cavities), and choice of stored current in an ultralow-emittance storage ring as well as some implications for brightness optimization.

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I. INTRODUCTION

Although already proposed in the 1990s [1–5], multibend achromat (MBA) lattices have only recently started to appear in storage ring-based light source designs [6–11]. The MBA lattice allows reaching ultralow emittance (i.e., transverse emittances substantially below 1 nm rad) and presents a path to fully diffraction-limited storage rings for the production of x-rays [12]. When the MAX IV facility [13,14] goes into operation in 2016, its 3 GeV storage ring will become the first ultralow-emittance storage ring based on a MBA [6,15]. Its 20-fold lattice employs a 7-bend achromat to achieve 328 pm rad transverse emittance with a circumference of 528 m. As is typical for such ultralow-emittance lattices, the radiative losses in the dipoles (364 keV/turn) are low compared to what can be expected (roughly 1 MeV/turn) once the ring is fully equipped with insertion devices (IDs) and/or damping wigglers (DWs). This can be recognized in Fig. 1 where various beam parameters are plotted as functions of the number of installed in-vacuum undulators (IVUs). As a consequence, the ring's zero-current emittance at any time depends on the type of installed IDs and their gap

settings. As the ID gaps vary during a typical user shift, not only will this change the transverse emittance [16], it will—assuming the rf cavities are not adjusted to compensate for gap motion—change the resulting rf acceptance, bunch length, and Touschek lifetime.

In addition, in medium-energy rings the large stored current along with the low transverse emittance leads to very strong intrabeam scattering (IBS) which blows up the beam's 6D emittance [17,18]. Hence, the resulting transverse emittance in ultralow-emittance storage rings at medium energies depends on the stored charge in the bunch. Specifically, the transverse emittance will decrease as the current drops. In state-of-the-art storage rings top-up injection is usually employed to prevent current decay, however, variations of stored charge from bunch to bunch are not uncommon and in certain cases actually desired (e.g., camshaft mode). In such situations, the emittance from bunch to bunch can vary as a function of bunch charge. Even if top-up injection and filling pattern control are used to ensure an even fill, the emittance can still vary as a result of ID gap motion and with it the amount of emittance blowup from IBS. Furthermore, a change of bunch energy spread (as a consequence of e.g., ID gap changes) or bunch length (rf cavity settings, harmonic cavity tuning, or ID gap changes), will also influence IBS and hence the resulting equilibrium emittance. The interplay between IDs, rf cavities, and transverse emittance via IBS will be the subject of Sec. II.

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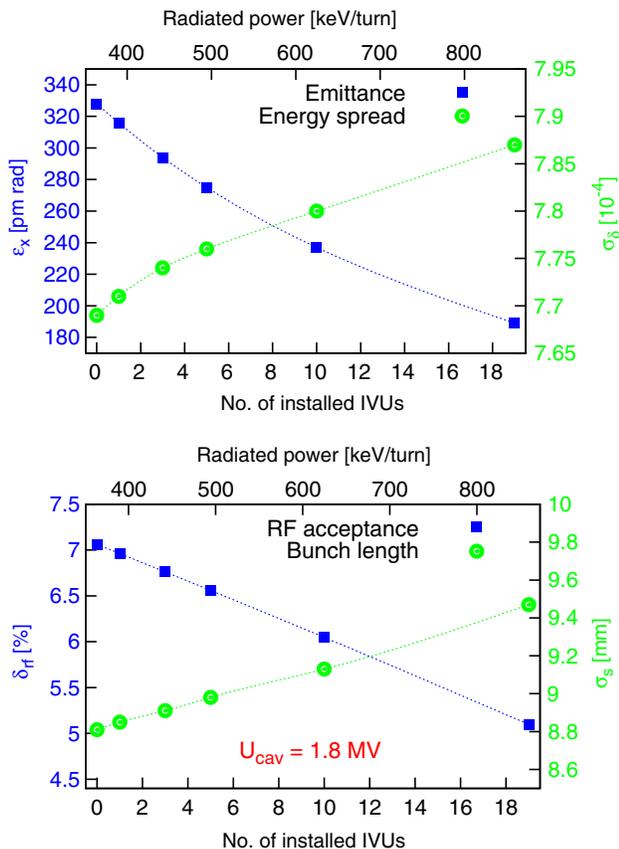


FIG. 1. Beam parameters of the MAX IV 3 GeV storage ring as a function of the number of installed IVUs (for details cf. Sec. II). At fully closed gap each IVU adds 26 keV/turn to the synchrotron radiation losses. Top: zero-current emittance and natural energy spread. Bottom: rf acceptance and zero-current bunch length assuming 1.8 MV overall cavity voltage.

Touschek lifetime [19,20] relies strongly on the 6D emittance: it grows with increasing longitudinal emittance which makes harmonic Landau cavities (LCs) for bunch lengthening attractive [21]. On the other hand, in the ultralow-emittance regime transverse momenta are small compared to the large momentum acceptance (MA) and, therefore, most scattering events do not transfer enough momentum from the transverse to the longitudinal to create Touschek losses. Instead, these events along with IBS lead to a blowup of the 6D emittance. Damping wigglers and IDs reduce the transverse emittance and can therefore increase the Touschek lifetime in ultralow-emittance storage rings. They also achieve this in another way: because their added losses reduce the available cavity overvoltage, they can lengthen the bunches which additionally increases Touschek lifetime. Furthermore, if they increase the energy spread in the bunch, the emittance blowup from IBS is reduced, which in turn also affects the resulting Touschek lifetime. The overall result is that the Touschek lifetime will vary as a function of resulting emittance including IBS as well as bunch lengthening. Since both of these factors are

determined by the type of installed IDs and momentary gap settings, the Touschek lifetime can vary during a typical user shift and needs to be calculated for each specific configuration and setting. This shall be investigated in Sec. III.

II. EMITTANCE AND INTRABEAM SCATTERING

As established in the Introduction, in MBA lattices with ultralow emittance, the resulting equilibrium emittance depends on the number and type of installed IDs (as well as their gap settings) and—at high stored current—is limited by IBS. This limitation can be recognized in Fig. 2 where the amount of emittance growth from IBS has been calculated assuming the lattice emittance could be varied freely. Regardless if LCs are employed to lengthen bunches or not, below ≈ 100 pm rad the resulting emittance becomes entirely dominated by IBS. The amount of emittance growth caused by IBS itself depends on the bunch charge and 6D bunch emittance. When an ID gap closes the transverse emittance of a bunch can be expected to decrease, while the bunch energy spread can be expected to grow. Furthermore, one must assume that the bunch length can be altered in this process. The result is that because of the gap change, the emittance blowup caused by IBS must be reevaluated.

The 6D tracking code TRACY-3 [22] has been used to calculate equilibrium emittances in all three planes taking into account IBS growth as a function of bunch charge and zero-current emittance. The code has implemented IBS calculations following the Bjorken-Mtingwa [23] as well as the Conte-Martini formalism [24] with the latter having

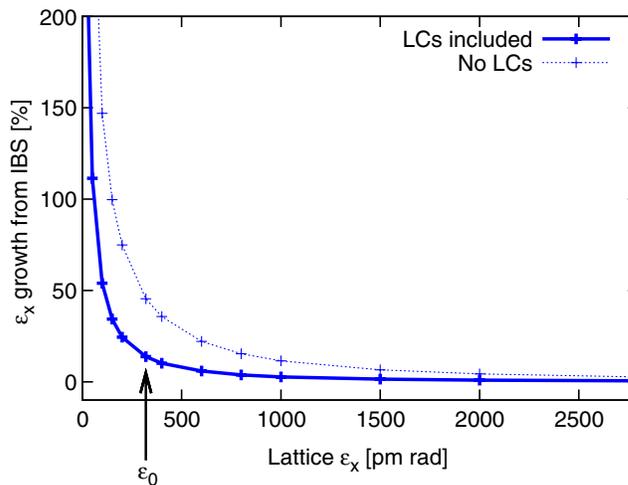


FIG. 2. Horizontal emittance growth caused by IBS at 500 mA stored current as a function of lattice emittance. It is assumed the latter can be adjusted freely while keeping the energy spread constant. The overall MA has been set to 4.5% and the vertical emittance is always adjusted to 8 pm rad. The effect of the LCs is shown. The equilibrium emittance ϵ_0 of the MAX IV 3 GeV storage ring bare lattice is indicated.

been benchmarked against ZAP [25,26]. In principle, for each ID and possible gap setting such a calculation has to be carried out. Because of the large number of possible combinations this is impractical. Instead, different lattice configurations of the MAX IV 3 GeV storage ring (where IDs, if included, are assumed to be operated with a fully closed gap) and different settings of emittance coupling have been studied: a bare lattice, a lattice with DWs, and a fully-equipped lattice, i.e., a lattice where an IVU has been installed in every available long straight. For the IVU, it is assumed that a typical device is 3.7 m long, has a magnetic period of 18.5 mm, and an effective magnetic field of 1.11 T [27] (adding 26 keV/turn losses). For the lattice with DWs, a total of four DWs has been added to the lattice. Each DW is 2 m long, has a period length of 80 mm and a peak magnetic field strength of 2.22 T [6] (adding 53 keV/turn losses). The emittance for the lattice with DWs is almost identical to that of a moderately ID-equipped lattice, i.e., a lattice where 10 IVUs have been installed. The calculations have been performed assuming two different settings of coupling [28]: one corresponding to the baseline 8 pm rad vertical emittance (1 Å diffraction limit) and one corresponding to a reduced coupling in order to increase photon brightness [29]. The results of these calculations are displayed in Table I. As IDs are added to the storage ring, the emittance decreases thus increasing the charge density and intensifying IBS. Note that since the rf cavities were assumed set to maximum accelerating voltage, the rf acceptances and natural bunch lengths vary between different configurations.

In addition to comparing zero-current emittances to emittances assuming 500 mA stored beam (in an even fill, i.e., 5 nC charge per bunch), results are also displayed where all bunches are assumed to be stretched by LCs [30]. Since LCs dilute the charge density in the bunch, they weaken IBS: even in a fully ID-equipped ring emittances of roughly 200 pm rad can still be achieved. Although LCs are employed in several 3rd generation storage rings to

TABLE I. Emittance (in pm rad) in the MAX IV 3 GeV storage ring for different settings of coupling and three lattice configurations: bare lattice, lattice with damping wigglers (equivalent to a moderately ID-equipped ring), and a fully ID-equipped ring. Emittance blowup from IBS with and without bunch lengthening from LCs was calculated assuming 500 mA stored current and rf cavities set to maximum voltage.

	Zero-current		IBS	IBS and LCs
	ϵ_y	ϵ_x	ϵ_x	ϵ_x
Bare	8	320	466	364
	2	326	552	404
DWs	8	226	354	264
	2	232	436	302
Loaded	8	179	292	213
	2	185	365	247

increase lifetime, they will be indispensable in the MAX IV 3 GeV storage ring to ensure ultralow emittance is preserved at full stored current.

The examples in Table I illustrate the large impact IDs have on the resulting emittance in ultralow-emittance rings based on MBA lattices. They also indicate that the emittance in such rings will not remain constant during user operation, but will vary as ID gaps are changed. In principle, one can consider operating DWs in order to counteract such emittance variations and ensure constant emittance during user shifts. However, since ID gaps are rarely ramped across their full range continuously during user shifts and since gap motion is usually not correlated between different beam lines, one can expect that emittance variations during user shifts should remain limited even without compensation by DWs.

It is also noteworthy that lowering the accelerating voltage in the main rf cavities can result in yet lower emittance. For the results presented in Table I, all cavities were assumed to be set to maximum accelerating voltage. This, however, means that the resulting bunch length is short and IBS becomes strongest. If the rf voltage is moderately reduced the bunch length increases limiting IBS. This shall be investigated in the next section.

III. MOMENTUM ACCEPTANCE AND LIFETIME

Achieving good Touschek lifetime depends on ensuring large MA. If the lattice MA is sufficient throughout the entire achromat and the rf cavities deliver enough accelerating voltage, the overall MA can become very large compared to the transverse momenta of the electrons in an ultralow-emittance storage ring. This ensures that Touschek lifetime in ultralow-emittance rings remains manageable despite the very high charge density in the bunch, and in fact, can improve when further lowering the transverse emittance. Therefore, ensuring large lattice MA has been one of the main goals of the nonlinear optics optimization for the MAX IV 3 GeV storage ring [6,15]. The requirement for the lattice MA was to match the provided rf acceptance [31] as well as possible. Figure 3 shows the lattice MA of the MAX IV 3 GeV storage ring bare lattice derived from 6D tracking with TRACY-3 for one synchrotron oscillation period. Tracking reveals that the lattice MA exceeds the minimum requirement of 4.5% throughout the entire achromat.

A. Touschek lifetime

With the lattice MA established, Touschek lifetime can be calculated as a function of rf acceptance, bunch charge and 6D emittance. This has been carried out with TRACY-3 [32] using the MAX IV 3 GeV storage ring as an example. Figure 4 shows results and confirms that the Touschek lifetime is high despite the ultralow emittance. Besides the behavior well known from 3rd generation light sources

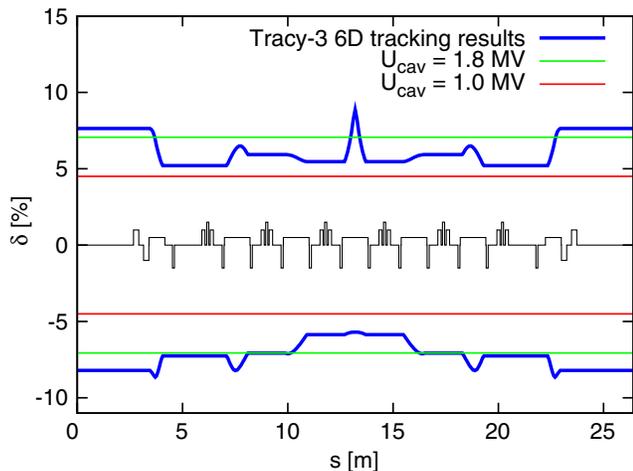


FIG. 3. Lattice MA for one achromat of the MAX IV 3 GeV storage ring. The solid blue line shows lattice MA from 6D tracking with TRACY-3 using actual vacuum chamber apertures. For comparison, the bare lattice rf acceptance is shown as well: cavities at maximum voltage 1.8 MV (7.1% rf acceptance) and at 1.0 MV (4.5% rf acceptance). The magnetic lattice is indicated at the center.

(above ≈ 1000 pm rad), one can recognize the entirely different behavior of ultralow-emittance rings (below ≈ 500 pm rad) where a sharp increase of Touschek lifetime occurs when the emittance is lowered. The MAX IV 3 GeV storage ring is clearly operated in this regime where Touschek lifetime can be expected to improve as IDs are added.

To investigate this, Touschek lifetime is calculated for different ID configurations of the storage ring as well as for

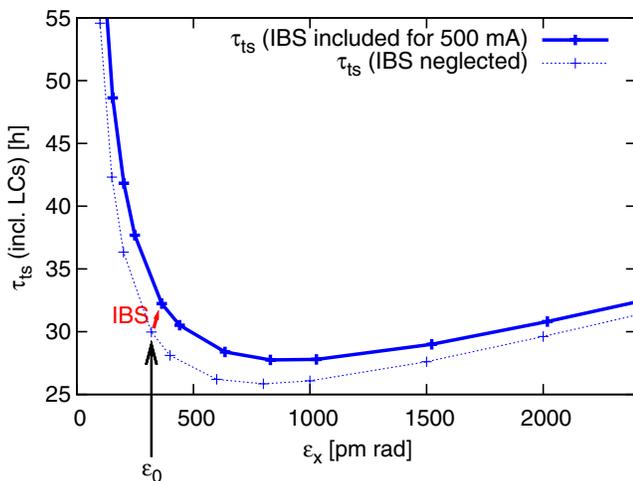


FIG. 4. Touschek lifetime (including the effect of LCs) from 6D tracking with TRACY-3 as a function of equilibrium emittance assuming the lattice emittance could be adjusted freely while keeping the energy spread constant. The overall MA has been set to 4.5% while the vertical emittance is adjusted to 8 pm rad. The effect of IBS at 500 mA stored current vs no IBS is displayed.

different settings of coupling in a self-consistent manner. In a first step, the zero-current emittance for a given lattice including IDs and rf cavity settings is calculated from the radiation integrals. From 6D tracking including vacuum apertures and possible imperfections such as field and multipole errors as well as misalignments, the local lattice MA around the ring is then derived. If LCs are employed, the 6D bunch emittance has to be updated to reflect the bunch lengthening. At this point, the IBS growth rates for a specific bunch charge and emittance are calculated. Iteration then allows finding the new equilibrium emittance. Finally, using the updated emittance, the Touschek lifetime can be calculated by integrating around the entire ring. Results of such tracking studies with TRACY-3 are displayed in Table II.

For a given setting of vertical emittance, there is a slight increase of Touschek lifetime when going from the bare lattice to the moderately ID-equipped ring. This is the result of two competing effects. The rf acceptance of the bare lattice case is larger increasing its Touschek lifetime. On the other hand, the bare lattice has a larger emittance which leads to lower lifetime (cf. Fig. 4). When going from the moderately ID-equipped lattice to the fully loaded ring, there is a substantial decrease of Touschek lifetime. This is again the result of two competing effects. The additional emittance reduction leads to a further Touschek lifetime increase. On the other hand, the rf acceptance is now considerably reduced (5.1% for the loaded ring vs the 6.1% of the moderately ID-equipped ring), so that the overall MA is more heavily dominated by the rf acceptance.

Since the lattice MA is large, the available rf acceptance has a strong influence on the Touschek lifetime. This is demonstrated in Fig. 5. Above 1.2 MV (corresponding to 5.2% rf acceptance) the lattice acceptance begins to dominate the overall MA and hence the lifetime starts to taper off. As the cavity voltage is further increased, the bunch length continues to reduce. Beyond 1.4 MV

TABLE II. Touschek lifetime (in hours) in the MAX IV 3 GeV storage ring for different settings of coupling and three lattice configurations (identical to those used in Table I). A stored current of 500 mA and rf cavities set to maximum voltage were assumed. The last column shows results where imperfections (misalignments, field and multipole errors) and reduced vertical acceptance from IVUs have been included in the model.

	ϵ_y [pm rad]	500 mA no LCs	500 mA including LCs	Including errors and narrow gaps ^a
Bare	8	17.4	87.1	64.3
	2	9.6	45.9	40.7
DWs	8	20.5	114.3	66.2
	2	10.4	56.1	48.7
Loaded	8	11.7	65.0	37.7
	2	5.8	31.4	27.3

^aNarrow gaps have not been included in the bare lattice case.

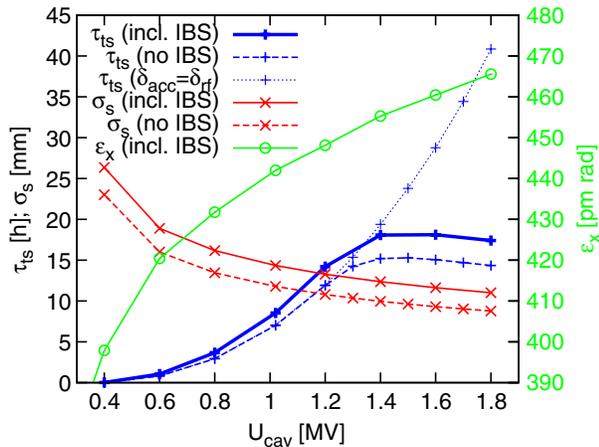


FIG. 5. Tauschek lifetime, bunch length, and horizontal emittance in the MAX IV 3 GeV storage ring bare lattice as functions of the rf cavity voltage. The stored current was assumed to be 500 mA with the vertical emittance always adjusted to 8 pm rad. Bunch lengthening from LCs has not been included.

(corresponding to 5.9% rf acceptance) this results in a decrease of Tauschek lifetime. However, a lifetime gain of up to 2–3 hours compared to the zero-current case can also be recognized as a result of the charge density dilution caused by IBS.

The example in Fig. 5 does not include bunch lengthening from LCs which are expected to be in use during user operation. Because LCs reduce the emittance blowup from IBS, the Tauschek lifetime can be increased further (cf. Fig. 4) compared to the result from bunch lengthening alone. Figure 6 shows how Tauschek lifetime increases with the bunch length while the emittance decreases.

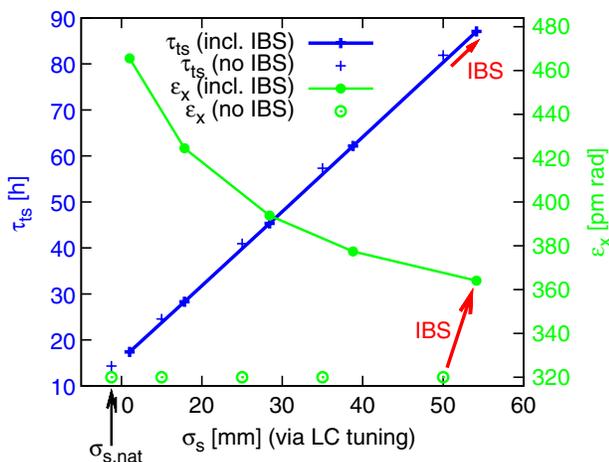


FIG. 6. Tauschek lifetime and horizontal emittance as functions of bunch length which is adjusted by tuning the LCs. The stored current was assumed to be 500 mA with the vertical emittance always set to 8 pm rad. The calculated Tauschek lifetime is based on resulting overall MA from tracking and actual vacuum apertures. The emittance blowup and bunch length increase from IBS as well as the associated lifetime increase are indicated.

B. Overall lifetime

To calculate the overall lifetime, the gas scattering lifetimes have to be added inversely to the Tauschek lifetime. However, in order to model a realistic machine, the Tauschek lifetime must also include the effect of imperfections which reduce the off-momentum dynamic aperture, as well as additional acceptance limitations imposed by the closed gaps of IVUs or by narrow-gap ID chambers. Results of such effects on the MAX IV 3 GeV storage ring are displayed in the last column of Table II. The vertical apertures in the long straights were reduced to ± 2 mm over a 4 m section of every long straight to model the acceptance limitation imposed by an IVU with closed gap. For the imperfections, 100 seeds were studied with field and multipole errors as well as misalignments. After alignment errors had been applied, orbit correction was simulated.

When all these effects are included, a Tauschek lifetime of 27.3 ± 2.1 h results even in the case of reduced rf acceptance (fully ID-equipped ring) and reduced vertical emittance. The uncertainty corresponds to one standard deviation of the error seeds. The gas scattering lifetimes in the MAX IV 3 GeV storage ring including in-vacuum IDs have been estimated at roughly 25 hours (elastic) and 56 hours (inelastic) where the latter has been calculated assuming a MA of only 4.5% [14]. The total lifetime should therefore always be above 10 h which is compatible with the foreseen top-up injection scheme with one top-up injection every few minutes ensuring a top-up deadband of about 0.5% [33]. For a moderately ID-equipped ring a Tauschek lifetime beyond 49 h can be expected depending on the choice of coupling. This corresponds to a total lifetime above 12 h. It is interesting to note that the lifetime in such a configuration is no longer Tauschek-dominated as is commonly the case in 3rd generation storage rings.

IV. CONCLUSIONS

Modern ultralow-emittance storage rings at medium energy are characterized by strong IBS and potentially large Tauschek lifetime if sufficient MA is provided by the lattice and rf system. Fully self-consistent tracking simulations are required to model the intricate interplay between the transverse and longitudinal emittances as a function of the bunch charge. Unlike existing 3rd generation storage rings, key parameters of these light sources will not remain constant during user shifts as they depend on continually varying ID gaps and the choice of rf cavity settings. In these rings one could therefore consider adding DWs specifically to enable adjusting the emittance to ensure constant electron beam dimensions during user shifts.

In these ultralow-emittance storage rings, LCs are both essential and versatile tools: besides mitigation of multi-bunch instabilities via Landau damping and bunch lengthening, they also preserve the ultralow emittance. As the examples in this paper show, good lifetime can be achieved despite the very low emittance through the application of

bunch lengthening LCs. Landau cavities are, however, also required in order to limit emittance growth from IBS thus preventing saturation of the achievable photon brightness at high bunch charge. Note also, that even in a fully diffraction-limited regime, the energy spread blowup caused by IBS can reduce the spectral brightness.

To further reduce the emittance and increase the Touschek lifetime of ultralow-emittance rings, one can contemplate adding additional DWs. Specifically, one could suggest starting to operate such light sources with DWs in all unoccupied user straights, removing a DW only when a user ID is ready to be installed in its place. Apart from the high cost (not only the initial cost of the DWs, but also the increased running cost that results from the high rf power consumption) of such a strategy, one should carefully analyze the resulting photon brightness. Meticulous DW design is required if the added energy spread shall not spoil any brightness gains from the reduced emittance.

Finally, it should be acknowledged that the strong emittance blowup from IBS is mainly an issue in medium-energy rings. Increasing the storage ring energy reduces the impact of IBS. The strong IBS in medium-energy ultralow-emittance rings is further compounded by low values of emittance coupling. The prospect of diffraction-limited storage rings operated at full coupling with round beams thus presents an interesting alternative.

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